

1. Use the formula

$$a + ar + ar^2 + ar^3 + \dots = \frac{a}{1 - r}$$

to compute the infinite sum

$$\frac{1}{3} + \frac{1}{3} \times \frac{1}{2} + \frac{1}{3} \times \left(\frac{1}{2}\right)^2 + \frac{1}{3} \times \left(\frac{1}{2}\right)^3 + \dots$$

2. Barney and Fred alternately flip a coin. The first one to get “heads” wins. If Barney goes first, what is the probability that he wins?
3. Solve for x : $x = \frac{2}{7} + \frac{5}{7}x^2$
4. Wilma and Betty play a series of games. The probability Wilma wins each game is $\frac{2}{7}$. What is the probability that Wilma will ever be up by one game?
5. Suppose instead the probability Wilma wins is $\frac{4}{9}$. What is the probability Wilma is ever up by one game?