

In class 2

Name: _____

Suppose $P(A) = \frac{1}{2}$, $P(B) = \frac{1}{3}$, $P(A|B) = \frac{3}{4}$

With this information we can find many more probabilities

1. By definition, $P(A|B) = \frac{P(A \cap B)}{P(B)}$. Therefore $P(A \cap B) =$
2. $P(A \cup B) = P(A) + P(B) - P(A \cap B)$. Therefore $P(A \cup B) =$
3. $P(B \cup A) =$
4. $P(A^c) =$
5. $P(B^c) =$
6. Since $P(B) = P(A \cap B) + P(A^c \cap B)$ we know $P(A^c \cap B) =$
7. Now we know all the numbers we need to find $P(A^c \cup B) = P(A^c) + P(B) - P(A^c \cap B)$

Here is another problem of the same type, but with different numbers:

Let $P(A) = .6$, $P(B) = .4$, $P(A \cap B) = .3$

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|--------------------|--------------------|-----------------------|
| 1. $P(A^c)$ | 6. $P(A \cap B^c)$ | 11. $P(A \cup B)$ |
| 2. $P(B^c)$ | 7. $P(A B^c)$ | 12. $P(A \cup B^c)$ |
| 3. $P(A B)$ | 8. $P(B^c A)$ | 13. $P(A^c \cup B)$ |
| 4. $P(B A)$ | 9. $P(B A^c)$ | 14. $P(A^c \cup B^c)$ |
| 5. $P(A^c \cap B)$ | 10. $P(A^c B)$ | |

